General Aptitude

Q. No. 1 – 5 Carry One Mark Each

1. Out of the following four sentences, select the most suitable sentence with respect to grammar and usage.
   (A) I will not leave the place until the minister does not meet me.
   (B) I will not leave the place until the minister doesn’t meet me.
   (C) I will not leave the place until the minister meet me.
   (D) I will not leave the place until the minister meets me.

   Key: (D)

2. A rewording of something written or spoken is a __________.
   (A) paraphrase     (B) paradox     (C) paradigm     (D) paraffin

   Key: (A)

3. Archimedes said, “Give me a lever long enough and a fulcrum on which to place it, and I will move the world.”
   The sentence above is an example of a __________ statement.
   (A) figurative     (B) collateral     (C) literal     (D) figurine

   Key: (A)

4. If ‘relftaga’ means carefree, ‘otaga’ means careful and ‘fertaga’ means careless, which of the following could mean ‘aftercare’?
   (A) zentaga     (B) tagafer     (C) tagazen     (D) relffer

   Key: (C)

5. A cube is built using 64 cubic blocks of side one unit. After it is built, one cubic block is removed from every corner of the cube. The resulting surface area of the body (in square units) after the removal is __________.
   (A) 56     (B) 64     (C) 72     (D) 96

   Key: (D)

   Exp: Four blocks are needed for each direction (totally 3 directions) to build a bigger cube containing 64 blocks. So area of one side of the bigger cube = $4 \times 4 = 16$ units.
   There are 6 faces so total area = $6 \times 16 = 96$ units.
   When cubes at the corners are removed they introduce new surfaces equal to exposes surfaces so the area of the bigger cube does not change from 96.

Q. No. 6 – 10 Carry Two Marks Each

+ India’s No.1 institute for GATE Training  ♦ 1 Lakh+ Students trained till date  ♦ 65+ Centers across India
173 per piece. The table below shows the numbers of each razor sold in each quarter of a year.

<table>
<thead>
<tr>
<th>Quarter \ Product</th>
<th>Elegance</th>
<th>Smooth</th>
<th>Soft</th>
<th>Executive</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q1</td>
<td>27300</td>
<td>20009</td>
<td>17602</td>
<td>9999</td>
</tr>
<tr>
<td>Q2</td>
<td>25222</td>
<td>19392</td>
<td>18445</td>
<td>8942</td>
</tr>
<tr>
<td>Q3</td>
<td>28976</td>
<td>22429</td>
<td>19544</td>
<td>10234</td>
</tr>
<tr>
<td>Q4</td>
<td>21012</td>
<td>18229</td>
<td>16595</td>
<td>10109</td>
</tr>
</tbody>
</table>

Which product contributes the greatest fraction to the revenue of the company in that year? (A) Elegance (B) Executive (C) Smooth (D) Soft

Key: (B)

7. Indian currency notes show the denomination indicated in at least seventeen languages. If this is not an indication of the nation’s diversity, nothing else is.

Which of the following can be logically inferred from the above sentences?
(A) India is a country of exactly seventeen languages.
(B) Linguistic pluralism is the only indicator of a nation’s diversity.
(C) Indian currency notes have sufficient space for all the Indian languages.
(D) Linguistic pluralism is strong evidence of India’s diversity.

Key: (D)

8. Consider the following statements relating to the level of poker play of four players P, Q, R and S.
I. P always beats Q
II. R always beats S
III. S loses to P only sometimes
IV. R always loses to Q

Which of the following can be logically inferred from the above statements?
(i) P is likely to beat all the three other players
(ii) S is the absolute worst player in the set
(A) (i) only   (B) (ii) only   (C) (i) and (ii)   (D) neither (i) nor (ii)

Key: (A)

9. If \( f(x^7) = 2x^7 + 3x - 5 \), which of the following is a factor of \( f(x) \)?
(A) \((x^3 + 8)\)        (B) \((x - 1)\)       (C) \((2x - 5)\)       (D) \((x + 1)\)
10. In a process, the number of cycles to failure decreases exponentially with an increase in load. At a load of 80 units, it takes 100 cycles for failure. When the load is halved, it takes 10000 cycles for failure. The load for which the failure will happen in 5000 cycles is ________.

(A) 40.00  (B) 46.02  (C) 60.01  (D) 92.02

Key: (B)

Exp: From the data given we assume

\[ \text{load} = \frac{\text{exponent}}{\log(\text{cycles})} \]

\[ 80 = \frac{x}{\log(10000)} \Rightarrow x = 160 \]

\[ 40 = \frac{x}{\log(10000)} \Rightarrow x = 160 \]

\[ \text{load} = \frac{160}{\log(5000)} = 43.25 \]

Civil Engineering

Q. No. 1 – 25 Carry One Mark Each

1. Newton-Raphson method is to be used to find root of equation \( 5x - e^x \cos x = 0 \). If the initial trial value for the root is taken as 0.333, the next approximation for the root would be __________.

(note: answer up to three decimal)

Key: (0.36)

Exp: Let \( f(x) = 3x - e^x + \sin x \) and \( x_0 = 0.333 \approx \frac{1}{3} \)

\[ f'(x) = 3 - e^x + \cos x \]

\[ f(x_0) = -0.069 \quad \text{and} \quad f'(x_0) = 2.55 \]

\[ x_1 = x_0 - \frac{f(x_0)}{f'(x_0)} \quad (\text{Using Newton-Raphson method}) \]

\[ = 0.333 + \frac{0.069}{2.55} = 0.360 \quad \text{is the required next approximation} \]

2. The type of partial differential equation \( \frac{\partial^2 P}{\partial x^2} + \frac{\partial^2 P}{\partial y^2} + 3 \frac{\partial^3 P}{\partial x \partial y} + 2 \frac{\partial P}{\partial x} - \frac{\partial P}{\partial y} = 0 \) is

(A) elliptic  (B) parabolic  (C) hyperbolic  (D) none of these
3. If the entries in each column of a square matrix $M$ add up to 1, then an eigen value of $M$ is
(A) 4  (B) 3  (C) 2  (D) 1

Key: (D)

Exp: Consider the ‘$2x^2$’ square matrix $M = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ Characteristic equation of $M$ is
\[ \lambda^2 - (a+d)\lambda + (ad-bc) = 0 \] ...(1)
Put $\lambda = 1$, we get
\[ 1-(a+d) + ad - bc = 0 \]
\[ 1-a - d + ad - (1-d)(1-a) = 0 \]
\[ 1-a - d + ad - 1 + a + d - ad = 0 \]
\[ 0 = 0 \] which is true

\[ \therefore \lambda = 1 \] Satisfies the equation (1) but $\lambda = 2, 3, 4$ does not satisfy the equation (1). For all possible values of $a, d$

Alternate Method: If sum of the elements in each row/column of a square matrix is equal to ‘S’ then ‘S’ is an eigen value of that matrix.

4. Type II error in hypothesis testing is
(A) acceptance of the null hypothesis when it is false and should be rejected
(B) rejection of the null hypothesis when it is true and should be accepted
(C) rejection of the null hypothesis when it is false and should be rejected
(D) acceptance of the null hypothesis when it is true and should be accepted

Key: (A)

Exp: Type II Errors means acceptance of the null hypothesis when it is false and should be rejected.

5. The solution of the partial differential equation $\frac{\partial u}{\partial t} = \alpha \frac{\partial^2 u}{\partial x^2}$ is of the form

(A) $Ce^{kt} \left[ C_1 e^{(\sqrt{k}/\alpha) x} + C_2 e^{-(\sqrt{k}/\alpha) x} \right]$ 
(B) $Ce^{kt} \left[ C_1 e^{(\sqrt{k}/\alpha) x} \right] + C_2 e^{-\sqrt{k}/\alpha}$
(C) $Ce^{kt} \left[ C_1 \cos \left( \frac{\sqrt{k}}{\alpha} x \right) + C_2 \sin \left( \frac{\sqrt{k}}{\alpha} x \right) \right]$
Exp: The P.D.E \( \frac{\partial u}{\partial t} = \alpha \frac{\partial^2 u}{\partial x^2} \) .... (1) is called 1-D heat equations.

Then the solution of (1) is

\[ u(x,t) = (A \cos \alpha x + B \sin \alpha x) \cdot e^{-\beta t} \]

Put \(-\beta^2 \alpha = k \Rightarrow \beta = \sqrt{\frac{k}{\alpha}} \cdot t \)

\[ \therefore \text{(1) becomes} \]

\[ u(x,t) = \left( A \cosh \sqrt{\frac{k}{\alpha}} x + B \sinh \sqrt{\frac{k}{\alpha}} x \right) C \cdot e^{kt} \]

\[ = C \cdot e^{kt} \left[ A \cdot \left( \frac{e^{\sqrt{\frac{k}{\alpha}} x}}{2} + \frac{e^{-\sqrt{\frac{k}{\alpha}} x}}{2} \right) + B \cdot \left( \frac{e^{\sqrt{\frac{k}{\alpha}} x}}{2} - \frac{e^{-\sqrt{\frac{k}{\alpha}} x}}{2} \right) \right] \]

\[ = C \cdot e^{kt} \left[ c_1 e^{\sqrt{\frac{k}{\alpha}} x} + c_2 e^{-\sqrt{\frac{k}{\alpha}} x} \right] \]

6. Consider the plane truss with load \( P \) as shown in the figure. Let the horizontal and vertical reactions at the joint B be \( H_B \) and \( V_C \).

Which one of the following sets gives the correct values of \( V_B, H_B \) and \( V_C \)?

(A) \( V_B = 0; H_B = 0; V_C = P \)

(B) \( V_B = P/2; H_B = 0; V_C = P/2 \)

(C) \( V_B = P/2; H_B = P (\sin 60^\circ); V_C = P/2 \)

(D) \( V_B = P; H_B = P (\cos 60^\circ); V_C = 0 \)

Key: (A)

Exp:

\[ \sum F_B = 0 \Rightarrow H_B = 0 \]

\[ \sum M_B = 0 \Rightarrow V_B \times 2L = 0 \Rightarrow V_B = 0 \]

\[ \sum V = 0 \Rightarrow V_C = P \]

7. In shear design of an RC beam, other than the allowable shear strength of concrete \( (\tau_c) \), there is also an additional check suggested in IS 456-2000 with respect to the maximum permissible shear stress \( (\tau_{c_{\text{max}}}) \). The check for \( \tau_{c_{\text{max}}} \) max is required to take care of

(A) additional shear resistance from reinforcing steel

(B) additional shear stress that comes from accidental loading
8. The semi-compact section of a laterally unsupported steel beam has an elastic section modulus, plastic section modulus and design bending compressive stress of 500 cm$^3$, 650cm$^3$ and 200MPa, respectively. The design flexural capacity (expressed in kNm) of the section is _______.  

Key: (100)  
Exp: As per IS 800, the design bending strength of laterally unsupported beam as governed by lateral torsional buckling is:  

$$M_d = \beta_b Z_p f_{bd}$$  

$$\beta_b = \frac{Z_c}{Z_p} \text{ for semi compact section,}$$  

So, $$M_d = \frac{Z_c}{Z_p} Z_p f_{bd} = Z_c f_{bd} = 500 \times 10^3 \times 200 \times 10^{-6} = 100 \text{kN} \cdot \text{m}$$

9. Bull's trench kiln is used in the manufacturing of  
   (A) Lime  
   (B) cement  
   (C) bricks  
   (D) none of these  

Key: (C)  

10. The compound which is largely responsible for initial setting and early strength gain of Ordinary Portland Cement is  
   (A) $C_3A$  
   (B) $C_2S$  
   (C) $C_3S$  
   (D) $C_4AF$  

Key: (B)  

11. In the consolidated undrained triaxial test on a saturated soil sample, the pore water pressure is zero  
   (A) during shearing stage only  
   (B) at the end of consolidation stage only  
   (C) both at the end of consolidation and during shearing stages  
   (D) under none of the above conditions  

Key: (B)  

12. A fine grained soil is found to be plastic in the water content range of 26-48%. As per Indian Standard Classification System, the soil is classified as  
   (A) CL  
   (B) CH  
   (C) CL-ML  
   (D) CI  

Key: (D)  
Exp: Soil is plastic in range of 26% to 48%. So, plastic limit =26%, liquid limit = 48%  
Since 35% <LL<50% So, CI
passive earth pressures, respectively, the maximum depth of unsupported excavation is

\[ (A) \frac{4c}{\gamma\sqrt{K_p}} \quad \frac{2c}{\gamma\sqrt{K_p}} \quad \frac{4c}{\gamma\sqrt{K_a}} \quad \frac{4c}{\gamma\sqrt{K_a}} \]

Key: (D)

Exp: \[ P_z = k_A \sigma_z - 2C_k \sqrt{k_A} \]

at \( z = z_0 \), \( P_z = 0 \)

\[ k_A (\gamma z_0) - 2C \sqrt{k_A} = 0 \]

\[ k_A (\gamma z_0) = 2C \sqrt{k_A} \]

\[ z_0 = \frac{2C \sqrt{k_A}}{\gamma k_A} = \frac{2C}{\gamma \sqrt{k_A}} \]

\[ Z_{critical} = 2z_0 = \frac{2 \times 2C}{\gamma \sqrt{k_A}} = \frac{4C}{\gamma \sqrt{k_A}} \]

14. The direct runoff hydrograph in response to 5 cm rainfall excess in a catchment is shown in the figure. The area of the catchment (expressed in hectares) is__

![Discharge vs. Time Graph]

Key: (21.6)

Exp: Area under hydrograph = direct runoff volume

\[ \frac{1}{2} \times 1 \times 6 \times 60 \times 60 = 5 \times \frac{1}{100} \times A \]

\[ \therefore 6 \times 60 \times 60 \times 100 = 2160000 \]
15. The type of flood routing (Group I) and the equation(s) used for the purpose (Group II) are given below.

<table>
<thead>
<tr>
<th>Group I</th>
<th>Group II</th>
</tr>
</thead>
<tbody>
<tr>
<td>P. Hydrologic flood routing</td>
<td>1. Continuity equation</td>
</tr>
<tr>
<td>Q. Hydraulic flood routing</td>
<td>2. Momentum equation</td>
</tr>
<tr>
<td></td>
<td>3. Energy equation</td>
</tr>
</tbody>
</table>

The correct match is

(A) P - 1; Q - 1, 2 & 3  
(B) P - 1; Q - 1 & 2  
(C) P - 1 & 2; Q - 1  
(D) P - 1 & 2; Q - 1 & 2

Key: (B)

16. The pre-jump Froude Number for a particular flow in a horizontal rectangular channel is 10. The ratio of sequent depths (i.e., post-jump depth to pre-jump depth) is \[ \frac{y_2}{y_1} \]

Key: (13.65)

Exp: Consider

Pre-jump depth = \( y_1 \)
Post-jump depth = \( y_2 \)
\( F_{r(j)} = 10 \)

We now that

\[ \frac{y_2}{y_1} = \frac{1}{2} \left[ \frac{y_1}{\sqrt{1 + 8F_{r(j)}^2 - 1}} \right] \]

\[ = \frac{1}{2} \left[ \sqrt{1 + 8 \times (10)^2} - 1 \right] \]

\[ = \frac{1}{2} \times 27.3 = 13.65 \]

17. Pre- cursors to photochemical oxidants are

(A) \( \text{NO}_x, \text{VOCs and sunlight} \)
(B) \( \text{SO}_2, \text{CO}_2 \) and sunlight
(C) \( \text{H}_2\text{S}, \text{CO} \) and sunlight
(D) \( \text{SO}_2, \text{NH}_3 \) and sunlight

Key: (A)

18. Crown corrosion in a reinforced concrete sewer is caused by:

(A) \( \text{H}_2\text{S} \)  
(B) \( \text{CO}_2 \)  
(C) \( \text{CH}_4 \)  
(D) \( \text{NH}_3 \)

Key: (A)

19. It was decided to construct a fabric filter, using bags of 0.45 m diameter and 7.5 m long, for removing industrial stack gas containing particulates. The expected rate of
20. Match the items in Group – I with those in Group – II and choose the right combination.

<table>
<thead>
<tr>
<th>Group - I</th>
<th>Group - II</th>
</tr>
</thead>
<tbody>
<tr>
<td>P. Activated sludge process</td>
<td>1. Nitrifiers and denitrifiers</td>
</tr>
<tr>
<td>Q. Rising of sludge</td>
<td>2. Autotrophic bacteria</td>
</tr>
<tr>
<td>R. Conventional nitrification</td>
<td>3. Heterotrophic bacteria</td>
</tr>
<tr>
<td>S. Biological nitrogen removal</td>
<td>4. Denitrifiers</td>
</tr>
</tbody>
</table>

(A) P-3, Q-4, R-2, S-1          
(B) P-2, Q- R-4, S-1  
(C) P-3, Q-2, R-4, S-1          
(D) P-1, Q-4, R-2, S-3

Key: (A)

21. During a forensic investigation of pavement failure, an engineer reconstructed the graphs P, Q, R and S, using partial and damaged old reports.

![Graphs P, Q, R, S](image)

Theoretically plausible correct graphs according to the 'Marshall mixture design output' are

(A) P, Q, R  
(B) P, Q, S  
(C) Q, R, S  
(D) R, S, P

Key: (B)
Exp: Maximum theoretical capacity, \( \frac{3600}{H_t} \) 
\[ = \frac{3600}{3} \]
\[ = 1200 \text{ veh/hr}. \]

23. The minimum number of satellites needed for a GPS to determine its position precisely is

(A) 2    (B) 3    (C) 4    (D) 24

Key: (C)

24. The system that uses the Sun as a source of electromagnetic energy and records the naturally radiated and reflected energy from the object is called

(A) Geographical Information System
(B) Global Positioning System
(C) Passive Remote Sensing
(D) Active Remote Sensing

Key: (C)

25. The staff reading taken on a workshop floor using a level is 0.645 m. The inverted staff reading taken to the bottom of a beam is 2.960 m. The reduced level of the floor is 40.500 m. The reduced level (expressed in m) of the bottom of the beam is

(A) 44.105    (B) 43.460    (C) 42.815    (D) 41.145

Key: (A)

Exp: \( \text{RL of bottom of beam} = 40.5 + 2.96 + 0.645 = 44.105 \text{m} \)

Q. No. 26 – 55 Carry Two Marks Each

26. Probability density function of a random variable \( X \) is given below

\[ f(x) = \begin{cases} 
0.25 & \text{if } 1 \leq x \leq 5 \\
0 & \text{otherwise} 
\end{cases} \]

\( P(X \leq 4) \) is

(A) \( \frac{3}{4} \)    (B) \( \frac{1}{2} \)    (C) \( \frac{1}{4} \)    (D) \( \frac{1}{8} \)

Key: (A)

Exp: \[ P(x \leq 4) = \int_{-\infty}^{4} f(x)dx = \int_{1}^{4} (0.25)dx + \int_{4}^{5} (0.25)dx + \int_{5}^{\infty} (0)dx \]
\[ = \frac{1}{4}(x)^4 \Big|_{1}^{4} = \frac{1}{4}(4-1) = \frac{3}{4} \]
27. The value of
\[ \int_0^\infty \frac{1}{1+x^2} \, dx + \int_0^\infty \frac{\sin x}{x} \, dx \]
is

(A) \( \frac{\pi}{2} \) \hspace{1cm} (B) \( \pi \) \hspace{1cm} (C) \( \frac{3\pi}{2} \) \hspace{1cm} (D) 1

Key: (B)

Exp: 
\[ \int_0^\infty \frac{1}{1+x^2} \, dx = \left[ \tan^{-1} x \right]_0^\infty = \tan^{-1} \infty - \tan^{-1} 0 = \frac{\pi}{2} \]

and \( L(\sin x) = \frac{1}{s^2+1} \Rightarrow L\left( \frac{\sin x}{x} \right) = \int_s^\infty \frac{1}{s^2+1} \, ds \) (Using "Division by x")

\[ = \left[ \tan^{-1} s \right]_0^\infty = \tan^{-1} \infty - \tan^{-1} (s) = \cot^{-1} (s) \]

\[ \Rightarrow \int_0^\infty e^{-sx} \frac{\sin x}{x} \, dx = \cot^{-1} (s) \] (Using definition of Laplace transform)

Put \( s=0 \), we get
\[ \int_0^\infty \frac{\sin x}{x} \, dx = \cot^{-1} (0) = \frac{\pi}{2} \]

\[ \infty \int_0^\infty \frac{1}{1+x^2} \, dx + \int_0^\infty \frac{\sin x}{x} \, dx = \pi \]

28. The area of the region bounded by the parabola \( y = x^2 + 1 \) and the straight line \( x+y = 3 \) is

(A) \( \frac{59}{6} \) \hspace{1cm} (B) \( \frac{9}{2} \) \hspace{1cm} (C) \( \frac{10}{3} \) \hspace{1cm} (D) \( \frac{7}{6} \)

Key: (B)

Exp: At the point of intersection of the curves, \( y = x^2+1 \) and \( x+y = 3 \) i.e., \( y=3-x \), we have
\[ x^2 + 1 = 3 - x \Rightarrow x^2 + x - 2 = 0 \]
\[ \Rightarrow x = -2, 1 \text{ and } 3 - x \geq x^2 + 1 \]
\[ \therefore \text{ Required area is } \frac{1}{2} \int_{-2}^{1} \left[ \frac{3-x}{2} + 1 \right] \, dx \]

\[ = \frac{1}{2} \int_{-2}^{1} \left[ \frac{3-x}{2} - (x^2 + 1) \right] \, dx \]

\[ = \left[ \frac{-x^3}{3} - \frac{x^2}{2} + 2x \right]_{-2}^{1} = \frac{9}{2} \]
29. The magnitudes of vectors \( \mathbf{P} \), \( \mathbf{Q} \) and \( \mathbf{R} \) are 100 kN, 250 kN and 150 kN, respectively as shown in the figure.

![Diagram of forces](image)

The respective values of the magnitude (in kN) and the direction (with respect to the x-axis) of the resultant vector are

(A) 290.9 and 96.0°  
(B) 368.1 and 94.7°  
(C) 330.4 and 118.9°  
(D) 400.1 and 113.5°  

**Key:** (C)

**Exp:** Resolving components w.r.t x-axis

\[
\sum F_x = P \cos 60° + \cos(60 + 45) + R \cos(90 + 45 + 60)
\]

\[
\sum F_x = 100 \cos 60° + 250 \cos 95° + 100 \cos 195°
\]

\[
\sum F_x = -159.6 \text{kN}
\]

\[
\sum F_y = P \sin 60° + Q \sin(60 + 45) + R \sin(90 + 45 + 60)
\]

\[
= 100 \sin 60° + 250 \sin 95° + 100 \sin 195°
\]

\[
\sum F_y = 289.3 \text{kN}
\]

\[
|F| = \sqrt{F_x^2 + F_y^2} = \sqrt{(-159.6)^2 + (289.3)^2} = 330.4 \text{kN}
\]

\[
\tan \theta = \frac{F_y}{F_x} = \frac{289.3}{-159.6} \Rightarrow \theta = -61.1°
\]

\(\theta, \text{w.r.t x-axis} = 180 - 61.1 = 118.9°\)

30. The respective expressions for complimentary function and particular integral part of the solution of the differential equation \( \frac{d^4y}{dx^4} + 3 \frac{d^2y}{dx^2} = 108x^2 \) are

(A) \( [c_1 + c_2 x + c_3 \sin \sqrt{3}x + c_4 \cos \sqrt{3}x] \) and \( [3x^4 - 12x^2 + c] \)

(B) \( [c_1 x + c_2 \sin \sqrt{3}x + c_4 \cos \sqrt{3}x] \) and \( [5x^4 - 12x^2 + c] \)

(C) \( [c_1 + c_3 \sin \sqrt{3}x + c_4 \cos \sqrt{3}x] \) and \( [3x^4 - 12x^2 + c] \)

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* India's No.1 institute for GATE Training  
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* 65+ Centers across India
Exp: D.E is \((D^4 + 3D^2)y = 108x^2, D = \frac{d}{dx}\)

A.E: \(- m^4 + 3m^2 = 0 \Rightarrow m^2(m^2 + 3) = 0 \Rightarrow m = 0, 0, \pm \sqrt{3}i\)

\[\therefore\text{ C.F} = (C_1 + C_2x) + C_3 \sin(\sqrt{3}x) + C_4 \cos(\sqrt{3}x)\]

and \[\text{P.I} = \frac{1}{D^4 + 3D^2}(108x^2) = \frac{1}{3D^2\left[1 + \frac{D^2}{3}\right]}(108x^2) = \frac{36}{D^2}\left[1 + \frac{D^2}{3}\right]^{-1}(x^2)\]

\[= \frac{36}{D^2}\left[1 - \frac{D^2}{3} + \ldots\right](x^2) = \frac{36}{D^2}\left[x^2 - \frac{1}{3}(2) + 0\right]\]

\[= \int \int \left(36x^2 - \frac{2}{3}\right)dx\,dx = 36\left(\frac{x^4}{4(3)} - \frac{2x^2}{3(2)} + 0\right) = 3x^4 - 12x^2\]

31. A 3 m long simply supported beam of uniform cross section is subjected to a uniformly distributed load of \(w = 20\) kN/m in the central 1 m as shown in the figure.

\[
w = 20 \text{ kN/m}
\]

in radians) of the deformed beam is

(A) \(0.681 \times 10^{-7}\)  
(B) \(0.943 \times 10^{-7}\)  
(C) \(4.310 \times 10^{-7}\)  
(D) \(5.91 \times 10^{-7}\)

Key: (*)

Exp:

\[
EI = 30 \times 10^6 \text{ N} \cdot \text{m}^2
\]

\[R_p = R_o = 10 \text{ kN}\]

\[M(x) = -EI \cdot \frac{d^2y}{dx^2} = 10x \quad (0 \leq x \leq 1)\]
0 ≤ x ≤ 1
\(-\frac{E.I.}{dx} = \frac{10x^2}{2} + C_1\)

0 ≤ y ≤ 0.5
\(-\frac{E.I.}{dx} = 10y - \frac{10}{3} y^3 + C_1\)

at y = 0.5; \(\frac{dy}{dx} = 0\)

\(\Rightarrow \frac{dy}{dx} = \frac{10 \times 0.5 - \frac{10}{3} \times (0.5)^3 + C_1}{0.5} = -4.583\)

\(\Rightarrow C_1 = -9.583\)

\(\Rightarrow \frac{dy}{dx}\bigg|_{y=0.5} = \frac{9.583}{30 \times 10^6} = -3.19 \times 10^{-7}\)

32. Two beams PQ (fixed at P and with a roller support at Q, as shown in Figure I, which allows vertical movement) and XZ (with a hinge at Y) are shown in the Figures I and II respectively. The spans of PQ and XZ are L and 2L respectively. Both the beams are under the action of uniformly distributed load \(W\) and have the same flexural stiffness, \(EI\) (where, \(E\) and \(I\) respectively denote modulus of elasticity and moment of inertia about axis of bending). Let the maximum deflection and maximum rotation be \(\delta_{max}\) and \(\theta_{max}\) respectively, in the case of beam PQ and the corresponding quantities for the beam XZ be \(\delta_{max2}\) and \(\theta_{max2}\) respectively.

Which one of the following
By principal of superposition,
\[ g_{\text{max,1}} = g_{\text{max,2}}; \theta_{\text{max,1}} = \theta_{\text{max,2}} \]

33. A plane truss with applied loads is shown in the figure.

The members which do not carry any force are
(A) FT, TG, HU, MP, PL
(B) ET, GS, UR, VR, QL
(C) FT, GS, HU, MP, QL
(D) MP, PL, HU, FT, UR

Key: (A)
Exp: Conditions for zero force members are
(i) The member meets at a joint and they are non-collinear and no external force acts at that joint. Both the members will be the zero force members.
(ii) When the members meet at joint and two are collinear and no external force acts at the joint then third member will be zero force member.

According to the above statements
We can say that
FT, TG, HU, MP and PL members are zero force members.

34. A rigid member ACB is shown in the figure. The member is supported at A and B by pinned and guided roller supports, respectively. A force P acts at C as shown. Let \( R_{ab} \)
Which one of the following sets gives the correct magnitudes of \( R_{Av}, R_{Bb}, \) and \( R_{Ah} \)?

(A) \( R_{Av} = 0; R_{Bb} = \frac{1}{3} P; \) and \( R_{Ah} = \frac{2}{3} P \)

(B) \( R_{Av} = 0; R_{Bb} = \frac{2}{3} P; \) and \( R_{Ah} = \frac{1}{3} P \)

(C) \( R_{Av} = P; R_{Bb} = \frac{3}{8} P; \) and \( R_{Ah} = \frac{1.5}{8} P \)

(D) \( R_{Av} = 0; R_{Bb} = \frac{1}{3} P; \) and \( R_{Ah} = \frac{2}{3} P \)

Key: (D)

Exp: Taking moments about \( A = 0 \)

\[ R_{Bb} \times 8 + P \times 1.5 = 0 \]

\[ R_{Bb} = \frac{-1.5P}{8} \]

\( \sum F_{II} = 0 \)

\[ R_{Ah} = R_{Bb} = \frac{1.5P}{8} \]

\( \sum F_{v} = 0 \)

\[ R_{Av} = P \]

35. A reinforced concrete (RC) beam with width of 250 mm and effective depth of 400 mm is reinforced with Fe415 steel. As per the provisions of IS 456-2000, the minimum and maximum amount of tensile reinforcement (expressed in mm\(^2\)) for the section are, respectively

(A) 250 and 3500

(B) 205 and 4000

(C) 270 and 2000

(D) 300 and 2500

Key: (B)

Exp: Given:

Width of beam \( b = 250\text{mm} \)

Effective depth \( d = 400\text{mm} \)

As per IS-456:2000

From clause 26.5.1.1 (a)

Minimum tension reinforcement

\[ A_s = 0.85 \]

\[ \frac{bd}{f_s} \]

\[ A = \frac{0.85bd}{0.85 \times 250 \times 400} = 0.85 \times 250 \times 400 = 204.819 \approx 205\text{mm}^2 \]
36. For M25 concrete with creep coefficient of 1.5, the long-term static modulus of elasticity (expressed in MPa) as per the provisions of IS:456-2000 is _____.

Key: (10000)

Exp: Long term elasticity = \( \frac{E_c}{1 + 0} \)

\[ E_c = 5000 \sqrt{f_{ck}} \]

\[ = 5000 \sqrt{25} \]

\[ = 500 \times 5 \]

\[ = 25000 \]

Creep coefficient \( (\theta) = 1.5 \)

long term elasticity = \( \frac{25000}{1 + 1.5} = 10,000 \)

37. A propped cantilever of span \( L \) carries a vertical concentrated load at the mid-span. If the plastic moment capacity of the section is \( M_p \), the magnitude of the collapse load is

(A) \( \frac{8M_p}{L} \)  
(B) \( \frac{6M_p}{L} \)

(C) \( \frac{4M_p}{L} \)  
(D) \( \frac{2M_p}{L} \)

Key: (B)

Exp: \(-M_p \theta - M_p \theta - M_p \theta + P \times \frac{L}{2} \theta = 0\)

\[ 3M_p \theta = \frac{PL \theta}{2} \]

\[ P = \frac{6M_p}{L} \]

38. Two plates are connected by fillet welds of size 10 mm and subjected to tension, as shown in the figure. The thickness of each plate is 12 mm. The yield stress and the ultimate tensile stress of steel are 250 MPa and 410 MPa, respectively. The welding is done in the workshop (\( \gamma_{sw} = 1.25 \)).
As per the Limit State Method of IS 800: 2007, the minimum length (rounded off to the nearest higher multiple of 5 mm) of each weld to transmit a force $P$ equal to 270 kN (factored) is

(A) 90 mm  (B) 105 mm  (C) 110 mm  (D) 115 mm

Key: (B)

Exp: Maximum force carried by plates,

$$P = \frac{A_y f_y}{\gamma_m} = \frac{100 \times 12 \times 250}{1.1} = 272.73 \text{kN}$$

Load carried by each weld $= \frac{P}{2} = 136.36 \text{kN}$

For minimum length of weld,

Strength of weld = Load carried by weld

$$l_w = \frac{f_u}{\sqrt{3} \gamma_{ml}} = 136.36 \times 10^3$$

$$l_w = (10 \times 0.7) \times \frac{410}{\sqrt{3} \times 1.2} = 136.36 \times 10^3$$

$$l_w = 102.99 \text{mm}$$

minimum multiple of 5 is

$\approx 105 \text{ mm}$

39. The Optimistic Time ($O$), most likely Time ($M$) and Pessimistic Time ($P$) (in days) of the activities in the critical path are given below in the form $O-M-P$.

```
E  8-10-14  F  6-8-11  G  5-7-10  H  7-12-18  I
```

Key: (37.83)

Exp: $t_c = \frac{8 + 4 \times 10 + 14}{6} + \frac{6 + 8 \times 4 + 11}{6} + \frac{5 + 7 \times 4 + 10}{6} + \frac{7 + 4 \times 12 + 18}{6}$

$$= 10.333 + 8.1666 + 7.1666 + 12.166$$

$$= 37.8328$$

40. The porosity ($\eta$) and the degree of saturation ($S$) of a soil sample are 0.7 and 40%, respectively. In a $100 \text{m}^3$ volume of the soil, the volume (expressed in $\text{m}^3$) of air is  

Key: (42)

Exp: $\eta = 0.7 = \frac{V_c}{V}$
S = 40\% = 0.40 = \frac{V_x}{V_v}

V = V_a + V_w + V_b \Rightarrow V_v + V_b V = \frac{V_v}{0.7}

V_v = 0.7V

0.40 = \frac{V_x}{V_v}

V_w = 0.4V_v

V_v - V_w = 0.4V_v

V_v - 0.4V_v = V_a

V_a = 0.6V_v

V_a = 0.6 \times 0.7V = 0.6 \times 0.7 \times 100

V_a = 42m^3

41. A homogeneous gravity retaining wall supporting a cohesionless backfill is shown in the figure. The lateral active earth pressure at the bottom of the wall is 40 kPa.

The minimum weight of the wall (expressed in kN per m length) required to prevent it from overturning about its toe (Point P) is

(A) 120  (B) 180  (C) 240  (D) 360

Key: (A)

Exp:
\[ \Rightarrow K_a \gamma H = 40 \Rightarrow K_a \gamma = \frac{40}{H} \]

So, \[ P_a = \frac{1}{2} K_a \gamma H^2 = 20H = 120 \text{kN} \]

Taking moment about \( P = 0 \)
\[ \Rightarrow P_a \times 2 = W \times 2 \]
\[ \Rightarrow P_a = W = 120 \text{kN} \]

42. An undisturbed soil sample was taken from the middle of a clay layer (i.e., 1.5 m below GL), as shown in the figure. The water table was at the top of the clay layer. Laboratory test results are as follows:

- Natural water content of clay: 25%
- Pre-consolidation pressure of clay: 60 kPa
- Compression index of clay: 0.50
- Recompression index of clay: 0.05
- Specific gravity of clay: 2.70
- Bulk unit weight of sand: 17 kN/m³

A compacted fill of 2.5 m height with unit weight of 20 kN/m³ is placed at the ground level.

Assuming unit weight of water as 10 kN/m³, the ultimate consolidation settlement (expressed in mm) of the clay layer is \( \text{___} \).

Key: (36.89)
For clay:

\[ w = 25\% = 0.25 \]
\[ es = wG \]
\[ e = \frac{wG}{s} = \frac{0.25 \times 2.7}{1} = 0.675 \]
\[ \gamma_{sub} = \gamma_{sat} - \gamma_w \]
\[ = \left( \frac{G + e}{1 + e} \right) \gamma_w - \gamma_w \]
\[ = \left( \frac{G - 1}{1 + e} \right) \gamma_w = \left( \frac{2.7 - 1}{1 + 0.675} \right) \times 10 = 10.15 \text{kN/m}^3. \]

\[ \bar{\sigma} \text{(Before Compaction)} = 17 \times 1 + 0.5 \times 10.15 = 17 + 5.075 = 22.075 \text{kN/m}^3 < \text{Pre consolidation pressure (60KPa)} \]

Hence Over consolidation stage

\[ \bar{\sigma} \text{ (After Compaction)} = 2.5 \times 20 + 17 \times 1 + 0.5 \times 10.15 = 50 + 17 + 5.075 = 72.075 \text{kN/m}^3 > 60 \text{kPa} \]

Hence Normal consolidation stage

Total settlement

\[ = \frac{C_R H_0}{1 + e_0} \log \left( \frac{\bar{\sigma}}{\sigma_0} \right) + \frac{C_e H}{1 + e_0} \log \left( \frac{\bar{\sigma}_o + \Delta \bar{\sigma}}{\bar{\sigma}_e} \right) \]

\[ C_R = 0.05 \]

\[ C_R = \frac{\Delta e}{\log \left( \frac{\bar{\sigma}_2}{\bar{\sigma}_1} \right)} = 0.05 \]

\[ \Delta e = 0.05 \log \left( \frac{60}{22.075} \right) \]

\[ \Delta e = 0.0217 \]

\[ 0.675 - e_0 = 0.0217 \]

\[ e_0 = 0.653 \Rightarrow \text{For overconsolidation stage} \]
\[
\Delta H = \frac{0.05 \times 1000}{1 + 0.653} \log \left( \frac{60}{22.075} \right) + \frac{0.5 \times 1000}{1 + 0.675} \log \left( \frac{72.075}{60} \right) \\
= 30.25 \times \log \left( \frac{60}{22.075} \right) + 298.5 \times \log \left( \frac{72.075}{60} \right) \\
= 30.25 \times 0.434 + 298.5 \times 0.0796 \\
= 13.13 + 23.76 \\
= 36.89 \text{ mm}
\]

43. A seepage flow condition is shown in the figure. The saturated unit weight of the soil \( \gamma_{\text{sat}} = 18 \ \text{kN/m}^3 \). Using unit weight of water, \( \gamma_w = 9.81 \ \text{kN/m}^3 \), the effective vertical stress (expressed in kN/m\(^2\)) on plane X-X is ___.

![Diagram of seepage flow condition]

Key: (65.475)

Exp: Effective stress at x-x, \( \sigma - u \)
\[
= 5 \times \gamma_{\text{sat}} + \frac{3}{6} \times 5 \gamma_w \\
= 5 \times (18 - 9.81) + 2.5 \times 9.81 \\
= 40.95 + 24.5 = 65.475 \text{ kN/m}^2
\]

44. A drained triaxial compression test on a saturated clay yielded the effective shear strength parameters as \( c' = 15 \ \text{kPa} \) and \( \phi' = 22^\circ \). Consolidated Undrained triaxial test on an identical sample of this clay at a cell pressure of 200 kPa developed a pore water pressure of 150 kPa at failure. The deviator stress (expressed in kPa) at failure is ___.

Key: (104.39)
C' = 15 KPa, \( \sigma_c = 200 \) KPa
\( \phi' = 22^\circ \), \( u = 150 \) KPa
\( \sigma_{c'} = \sigma_c - u = 200 - 150 = 50 \) KPa

We know that
\( \sigma_{tr} = \sigma_{c'} + \sigma_d' \)
\( \sigma_{tr} = 50 \) KPa

\( \sigma_{tr} = \sigma_{3l} N_d + 2C \sqrt{N_d} \)

\( N_d = \tan^2 \left( 45 + \frac{\phi'}{2} \right) = \tan^2 \left( 45 + \frac{22}{2} \right) = \tan^2 (45 + 11) = \tan^2 (56) = 2.198 \)

\( \sigma_{tr} = 50 \times 2.198 + 2 \times 15 \times \sqrt{2198} \)
\( = 109.9 + 30 \times (1.483) \)
\( = 109.9 + 44.49 = 154.39 \)

\( \sigma_{tr} = 154.39 \)
\( \sigma_{c'} + \sigma_d' = 154.39 \)
\( \sigma_d' = 154.39 - \sigma_c' = 154.39 - 50 \)

Deviator stress \( \sigma_d' = 104.39 \)

45. A concrete gravity dam section is shown in the figure. Assuming unit weight of water as 10 kN/m\(^3\) and unit weight of concrete as 24 kN/m\(^3\), the uplift force per unit length of the dam (expressed in kN/m) at PQ is ______.

Key: (10500)
Exp: \[ \gamma_w \times H_1 \]
\[= 10 \times 65 = 650 \text{kN} / \text{m}^2 \]
\[\gamma_w H_2 + \frac{1}{3} \gamma_w (H_2 - H_1)\]
\[= 50 + \frac{1}{3} \times 10 \times 60 = 250 \text{kN} / \text{m}^2 \]
\[P = \frac{1}{2} \times (650 + 250) \times 10 + \frac{1}{2} \times (250 + 50) \times 40\]
\[= 4500 + 6000\]
\[= 10500 \text{kN} / \text{m} \]

46. Seepage is occurring through a porous media shown in the figure. The hydraulic conductivity values \((k_1, k_2, k_3)\) are in m/day.

The seepage discharge \((\text{m}^3/\text{day per m})\) through the porous media at section PQ is

(A) \(\frac{7}{12}\)  
(B) \(\frac{1}{2}\)  
(C) \(\frac{9}{16}\)  
(D) \(\frac{3}{4}\)

Key: (B)

Exp: Flow is normal to bedding flame
\[K_{\text{avg}} = \frac{\sum z_1}{\sum k_1} = \frac{20 + 30 + 10}{3 + 3 + 1} = 2 \text{ m/day} \]
\[i = \frac{\text{Head difference}}{\text{Length}} = \frac{15 - 10}{60} = \frac{5}{60} = \frac{1}{12} \]
Seepage discharge \(q = K_{\text{avg}} \times i \times A = 2 \times \frac{1}{12} \times 3 \times 1 = 0.5 \text{m}^3 / \text{day} / \text{m} \)
47. A 4 m wide rectangular channel, having bed slope of 0.001 carries a discharge of 16 m$^3$/s. Considering Manning's roughness coefficient = 0.012 and $g = 10$ m/s$^2$, the category of the channel slope is

(A) Horizontal   (B) mild   (C) critical   (D) steep

Key: (B)

Exp: Given discharge ($Q$) = 16 m$^3$/sec.
Bed slope ($S$) = 0.001
Manning's roughness coefficients ($n$) = 0.012
$g = 10$ m/s$^2$
Width ($B$) = 4 m
Channel is wide rectangular

\[
\begin{array}{c}
\text{y} \\
\text{B} \\
\text{B} \\
y \gg \text{y}
\end{array}
\]

Area ($A$) = $B$. $y$
Perimeter ($P$) = $B$

Hydraulic Radius ($R$) = \( \frac{A}{P} = \frac{By}{B} = y \)

\[
Q = \frac{A}{n} R^{\frac{2}{3}} S^{\frac{1}{2}}
\]

\[
16 = \frac{1}{0.02} (4 \times y) y^{2/3} S^{1/2}
\]

For meaning equation

\[
\frac{16 \times 0.012}{4 \times \sqrt{0.001}} = y^{5/3}
\]

\[
y = 2.95 \text{m}
\]

\[
y_e = \left( \frac{Q}{g} \right)^{1/3}
\]

\[
q = \frac{Q}{B} = \frac{16}{4} = 4
\]

\[
y_e = 1.169 \text{m}
\]

\[y > y_e \Rightarrow \text{Channel is mild slope.}\]
Key: \( (127) \)

**Exp:**

\[
F_\Pi = \frac{1}{2} \times \frac{1000 \times 10 \times (5)^2}{1000} \text{ KN} = 125 \text{kN}
\]

\( F_\Pi \) acts at a distance \( \frac{5}{3} = 1.67 \text{ m} \) from the base.

\( F_\nu = \text{Weight of water enclosed or supported (actual or imaginary) by the curved surface} = \rho g \times \text{Vacuum of portion ABC} \)

\[
= 1000 \times 10 \times \left[ \frac{1}{2} \times \frac{25}{180} \times \pi - 2 \times \frac{1}{2} \times \frac{5}{2} \times \frac{5\sqrt{3}}{2} \right]
\]

\[
= 1000 \times 10 \times \left[ \frac{25}{6} \times \pi - 1.25 \times 5\sqrt{3} \right]
\]

\[
= 1000 \times 10 \times 2.27 \times 1 \text{N}
\]
49. A hydraulically efficient trapezoidal channel section has a uniform flow depth of 2m. The bed width (expressed in m) of the channel is ______.

Key: (2.3)

Exp:

For Hydraulically efficient channel,

\[ B = \frac{2}{\sqrt{3}} \times \frac{2}{\sqrt{3}} \times 2 = \frac{4}{\sqrt{3}} = 2.31 \text{ m} \]

50. Effluent from an industry 'A' has a pH of 4.2. The effluent from another industry 'B' has double the hydroxyl (OH\(^{-}\)) ion concentration than the effluent from industry 'A'. pH of effluent from the industry 'B' will be ______

Key: (4.5)

Exp:

A

\[ p^H = 4.2, \quad p^{\text{OH}} = 9.8, \]

\[ \Rightarrow [\text{OH}^-] = 10^{-9.4} \text{ mol/L} \]

B

\[ [\text{OH}^-] = 2 \times 10^{-9.8} \text{ mol/L} \]

\[ \Rightarrow p^{\text{OH}} = 9.8 - \log_{10} 2 = 9.5 \]

\[ \Rightarrow p^H = 4.5 \]

51. An electrostatic precipitator (ESP) with 5600 m\(^2\) of collector plate area is 96 percent efficient in treating 185 m\(^3\)/s of flue gas from a 200 MW thermal power plant. It was found that in order to achieve 97 percent efficiency, the collector plate area should be 6100 m\(^2\). In order to increase the efficiency to 99 percent, the ESP collector plate area (expressed in m\(^2\)) would be __________

Key: (8011.8)

Exp:

\[ A = \frac{Q}{\text{we}} \ln (1 - \eta) \]

\[ S_0 = \frac{A_1}{A_2} = \frac{S_1}{S_2} \]
\[
\Rightarrow \frac{5600}{\ln(1-9.6)} = \frac{A}{\ln(1-0.99)} \\
\Rightarrow A = 8011.8 \text{m}^2
\]

52. The 2-day and 4-day BOD values of a sewage sample are 100 mg/L and 155 mg/L, respectively. The value of BOD rate constant (expressed in per day) is ___.

Key: (0.3)

Exp: \[ \text{BOD}_2 = L_0 \times (1 - e^{-k \cdot 2}) \]
\[
\Rightarrow 100 = L_0 \times (1 - e^{-2k})
\]
\[
\text{Also, } 155 = L_0 \times (1 - e^{-4k})
\]
\[
(i) / (ii)
\]
\[
\frac{100}{155} = \frac{1 - e^{-2k}}{1 - e^{-4k}}
\]
\[
1 - e^{-4k} = 1.55 - 1.55 \times e^{-2k}
\]
\[
e^{-4k} = 1.55 - 1.55 \times e^{-2k} + 0.55 = 0
\]
Let \(e^{-2k} = x\)
\[
x^2 - 1.55x + 0.55 = 0
\]
\[
x = 0.55
\]
\[
e^{-2k} = -0.55 \Rightarrow k = 0.2 \text{ day}^{-1}
\]

53. A two lane, one-way road with radius of 50 m is predominantly carrying lorries with wheelbase of 5 m. The speed of lorries is restricted to be between 60 kmph and 80 kmph. The mechanical widening and psychological widening required at 60 kmph are designated as \(w_{\text{me},60}\) and \(w_{\text{ps},60}\), respectively. The mechanical widening and psychological widening required at 80 kmph are designated as \(w_{\text{me},80}\) and \(w_{\text{ps},80}\), respectively. The correct values of \(w_m\) and \(w_p\) respectively are

(A) 0.89 m, 0.50 m, 1.19 m, and 0.50 m

(B) 0.50 m, 0.89 m, 0.50 m, and 1.19 m

(C) 0.50 m, 1.19 m, 0.50 m, and 0.89 m

(D) 1.19 m, 0.50 m, 0.89 m, and 0.50 m

Key: (B)

Exp: \[ W_{\text{me},\text{for } 60\text{kmph}} = \frac{1}{2R} = \frac{2 \times (5)^2}{2 \times 50} = 0.5 \text{m} \]
\[ W_{\text{ps},\text{for } 60\text{kmph}} = \frac{V}{9.5 \sqrt{R}} = \frac{60}{9.5 \times \sqrt{50}} = 0.89 \text{m} \]
\[ W_{\text{ps},\text{for } 80\text{kmph}} = \frac{2 \times (5)^2}{9.5 \times \sqrt{50}} = 0.5 \text{m} \]
54. While traveling along and against the traffic stream, a moving observer measured the relative flows as 50 vehicles/hr and 200 vehicles/hr, respectively. The average speeds of the moving observer while traveling along and against the stream are 20 km/hr and 30 km/hr, respectively. The density of the traffic stream (expressed in vehicles/km) is _________.

Key: (3)

55. The vertical angles subtended by the top of a tower T at two instrument stations set up at P and Q, are shown in the figure. The two stations are in line with the tower and spaced at a distance of 60 m. Readings taken from these two stations on a leveling staff placed at the benchmark (BM = 450.000 m) are also shown in the figure. The reduced level of the top of the tower T (expressed in m) is _________.

Key: (476.9)

Exp:

\[ \Delta TST; \tan 16.5^\circ = \frac{T'T}{x} \quad \text{(i)} \]

\[ \Delta TRT'', \tan 10.5^\circ = \frac{T''T}{x + 60} = \frac{T'T + 2}{x + 60} \quad \text{(ii)} \]

From (i) and (ii)

\[ x \times \tan 16.5^\circ = (x + 10) \times \tan (10.5^\circ) - 2 \]
\[ \Rightarrow x \times 0.296 = (x + 10) \times 0.185 - 2 \]
\[ \Rightarrow x = 82.25 \text{ m} \]

So, \( T'T = 82.25 \times 0.296 = 24.35 \text{ m} \)

So, RL of top of tower = 450 + 2.555 + 24.35 = 476.905 m
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